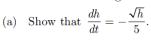
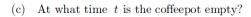
Related Rates Review II

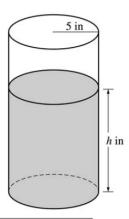
Question 5

A coffeepot has the shape of a cylinder with radius 5 inches, as shown in the figure above. Let h be the depth of the coffee in the pot, measured in inches, where h is a function of time t, measured in seconds. The volume V of coffee in the pot is changing at the rate of $-5\pi\sqrt{h}$ cubic inches per second. (The volume V of a cylinder with radius r and height h is $V = \pi r^2 h$.)



(b) Given that h=17 at time t=0, solve the differential equation $\frac{dh}{dt}=-\frac{\sqrt{h}}{5}$ for h as a function of t.





AP® CALCULUS AB 2008 SCORING GUIDELINES

Question 3

Oil is leaking from a pipeline on the surface of a lake and forms an oil slick whose volume increases at a constant rate of 2000 cubic centimeters per minute. The oil slick takes the form of a right circular cylinder with both its radius and height changing with time. (Note: The volume V of a right circular cylinder with radius r and height h is given by $V = \pi r^2 h$.)

- (a) At the instant when the radius of the oil slick is 100 centimeters and the height is 0.5 centimeter, the radius is increasing at the rate of 2.5 centimeters per minute. At this instant, what is the rate of change of the height of the oil slick with respect to time, in centimeters per minute?
- (b) A recovery device arrives on the scene and begins removing oil. The rate at which oil is removed is $R(t) = 400\sqrt{t}$ cubic centimeters per minute, where t is the time in minutes since the device began working. Oil continues to leak at the rate of 2000 cubic centimeters per minute. Find the time t when the oil slick reaches its maximum volume. Justify your answer.
- (c) By the time the recovery device began removing oil, 60,000 cubic centimeters of oil had already leaked. Write, but do not evaluate, an expression involving an integral that gives the volume of oil at the time found in part (b).

AP[®] CALCULUS AB 2009 SCORING GUIDELINES (Form B)

Question 1

At a certain height, a tree trunk has a circular cross section. The radius R(t) of that cross section grows at a rate modeled by the function

$$\frac{dR}{dt} = \frac{1}{16} (3 + \sin(t^2))$$
 centimeters per year

for $0 \le t \le 3$, where time t is measured in years. At time t = 0, the radius is 6 centimeters. The area of the cross section at time t is denoted by A(t).

- (a) Write an expression, involving an integral, for the radius R(t) for 0 ≤ t ≤ 3. Use your expression to find R(3).
- (b) Find the rate at which the cross-sectional area A(t) is increasing at time t = 3 years. Indicate units of measure.
- (c) Evaluate $\int_0^3 A'(t) dt$. Using appropriate units, interpret the meaning of that integral in terms of cross-sectional area.