Factor the following completely under the Real Domain:

1. 
$$x^4 - 16$$

2. 
$$x^3 + x^2 - x - 1$$

3. 
$$x^3 - 125$$

4. 
$$27x^6 + 8y^3$$

Divide using long division:

5. 
$$\frac{x^4 - x^3 + 3x^2 - 3x + 2}{x - 6}$$
  
6. 
$$\frac{2x^5 - 4x^4 + 6x^2 - 3x + 2}{x^2 + x - 4}$$

Divide using synthetic division:

7. 
$$\frac{x^6 - 2x^4 - 3x^3 + x^2 - 3x - 5}{x + 3}$$

8. Use the remainder theorem to find the remainder of  $5x^3 + 2x^2 - 3x - 14$  when x = -2.

9. Use the factor theorem to determine whether or not -1 is a factor of  $8x^4 - 3x^3 + 2x^2 - 3x - 16$ 

10. Decide if x + 2 is a factor of  $f(x) = 3x^3 - 13x^2 - 18x + 40$ . If so, Write f(x) as a product of its linear factors.