

## Irrational and Imaginary Root Theorems

**State the number of complex zeros and the possible number of real and imaginary zeros for each function.**

1)  $f(x) = x^2 + 6x - 38$

2)  $f(x) = x^4 - 9x^2 + 18$

3)  $f(x) = 5x^5 + 36x^3 + 7x$

4)  $f(x) = 3x^3 + 2x^2 - x$

5)  $f(x) = 27x^6 + 208x^3 - 64$

6)  $f(x) = 27x^9 + 8x^6 - 27x^3 - 8$

**A polynomial function with rational coefficients has the follow zeros. Find all additional zeros.**

7)  $-5, i$

8)  $-1 + i, \sqrt{5}$

9)  $-3 + \sqrt{5}, -i$

10)  $2, -2 + \sqrt{10}$

11)  $-1, 5, -2 + \sqrt{5}$

12)  $2 - 2i, 1 - 2i, 1 + 2i$

13)  $2 - 3i$  mult. 2

14)  $-\frac{5}{2}, \sqrt{5}$  mult. 2

**Write a polynomial function of least degree with integral coefficients that has the given zeros.**

15) 0, 2,  $\sqrt{3}$

16) -5,  $\sqrt{3}$

17) -1,  $2i$

18)  $2i, -2i, 2 + 2i$

19)  $-2i, 2 + 2\sqrt{2}$

20)  $\sqrt{6}, -3 + \sqrt{5}$

**Critical thinking questions:**

21) Write a polynomial function of fifth degree with integral coefficients that has  $2i$  as a zero.

22) True or False: A polynomial function of third degree with integral coefficients can have 2 and  $2i$  as zeros.

## Irrational and Imaginary Root Theorems

State the number of complex zeros and the possible number of real and imaginary zeros for each function.

1)  $f(x) = x^2 + 6x - 38$

# of complex zeros: 2

Possible # of real zeros: 2 or 0

Possible # of imaginary zeros: 2 or 0

2)  $f(x) = x^4 - 9x^2 + 18$

# of complex zeros: 4

Possible # of real zeros: 4, 2, or 0

Possible # of imaginary zeros: 4, 2, or 0

3)  $f(x) = 5x^5 + 36x^3 + 7x$

# of complex zeros: 5

Possible # of real zeros: 5, 3, or 1

Possible # of imaginary zeros: 4, 2, or 0

4)  $f(x) = 3x^3 + 2x^2 - x$

# of complex zeros: 3

Possible # of real zeros: 3 or 1

Possible # of imaginary zeros: 2 or 0

5)  $f(x) = 27x^6 + 208x^3 - 64$

# of complex zeros: 6

Possible # of real zeros: 6, 4, 2, or 0

Possible # of imaginary zeros: 6, 4, 2, or 0

6)  $f(x) = 27x^9 + 8x^6 - 27x^3 - 8$

# of complex zeros: 9

Possible # of real zeros: 9, 7, 5, 3, or 1

Possible # of imaginary zeros: 8, 6, 4, 2, or 0

A polynomial function with rational coefficients has the follow zeros. Find all additional zeros.

7)  $-5, i$

 $-i$ 

8)  $-1 + i, \sqrt{5}$

 $-1 - i, -\sqrt{5}$ 

9)  $-3 + \sqrt{5}, -i$

 $-3 - \sqrt{5}, i$ 

10)  $2, -2 + \sqrt{10}$

 $-2 - \sqrt{10}$ 

11)  $-1, 5, -2 + \sqrt{5}$

 $-2 - \sqrt{5}$ 

12)  $2 - 2i, 1 - 2i, 1 + 2i$

 $2 + 2i$

13)  $2 - 3i$  mult. 2

$2 + 3i$  mult. 2

14)  $-\frac{5}{2}, \sqrt{5}$  mult. 2

$-\sqrt{5}$  mult. 2

Write a polynomial function of least degree with integral coefficients that has the given zeros.

15) 0, 2,  $\sqrt{3}$

$f(x) = x^4 - 2x^3 - 3x^2 + 6x$

16) -5,  $\sqrt{3}$

$f(x) = x^3 + 5x^2 - 3x - 15$

17) -1,  $2i$

$f(x) = x^3 + x^2 + 4x + 4$

18)  $2i, -2i, 2 + 2i$

$f(x) = x^4 - 4x^3 + 12x^2 - 16x + 32$

19)  $-2i, 2 + 2\sqrt{2}$

$f(x) = x^4 - 4x^3 - 16x - 16$

20)  $\sqrt{6}, -3 + \sqrt{5}$

$f(x) = x^4 + 6x^3 - 2x^2 - 36x - 24$

### Critical thinking questions:

21) Write a polynomial function of fifth degree with integral coefficients that has  $2i$  as a zero.

Many answers. Ex:  $f(x) = x^5 + 4x^3$

22) True or False: A polynomial function of third degree with integral coefficients can have 2 and  $2i$  as zeros.

True