

Riemann Sum

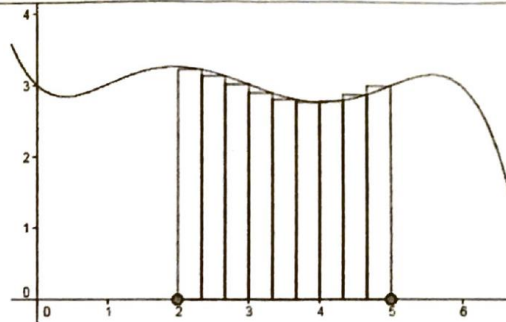
Use table for #'s 1-2. Find the following Riemann sum for the given n based on the given table of values:
Left, Right, Midpoint, and Trapezoidal.

| | | | | | | | | | |
|--------|---|---|---|----|----|----|----|----|----|
| x | 0 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 |
| $f(x)$ | 3 | 5 | 9 | 14 | 15 | 19 | 25 | 28 | 30 |

- $n = 2$
- $n = 4$
- Looking at the values given, does R_L under or over approximate compared the actual area under the curve?
- Given $f(x) = x^2$, Find all 4 Riemann sums with $n=6$ in the interval from $[1,4]$.
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Use the graph to answer 1-3.

- Is the rectangular approximation shown to the right a left endpoint, right endpoint, or midpoint approximation?
- Is the approximation less than or greater than the true value?
- What is the width of each rectangle?



6.

Use the information provided to answer the following.

11. Let $y(t)$ represent the rate of change of the population of a town over a 20-year period, where y is a differentiable function of t . The table shows the population change in people per year recorded at selected times.

| | | | | | |
|--|------|------|------|------|------|
| Time (years) | 0 | 4 | 10 | 13 | 20 |
| $y(t)$ (people per year) | 2500 | 2724 | 3108 | 3697 | 4283 |

- Use the data from the table and a right Riemann Sum with four subintervals to approximate the area under the curve.
- What does your answer from part (a) represent?
- Assuming that $y(t)$ is a continuous increasing function, is your approximation from part (a) greater or less than the true value?